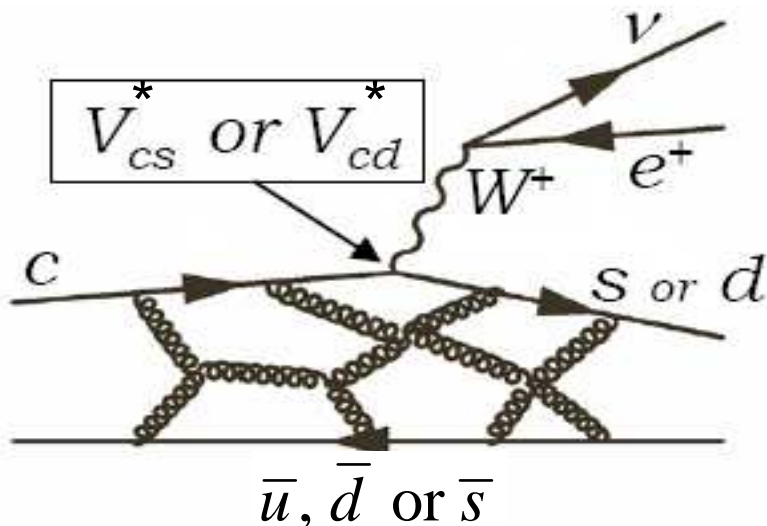
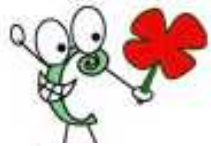


# Semileptonic Decays with CLEO-c

charm

*Beauty 2009*  
*07-11 September 2009*



- Introduction
- Analysis techniques
- $D$  and  $D_s$  Semileptonic:  
Branching fractions  
Semileptonic form factors  
CKM ( $|V_{cs}|$ ,  $|V_{cd}|$  and more)
- Summary and prospects

Presented by Patrick Spradlin  
University of Oxford

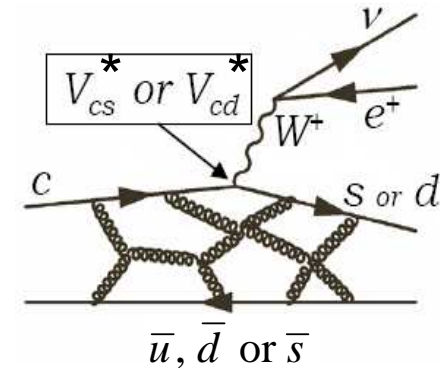
On behalf of the CLEO collaboration  
*Slides kindly provided by Bo Xin and Ian Shipsey*

# Importance of Charm Semileptonic Decays

- Golden  $P \rightarrow P$  transitions:

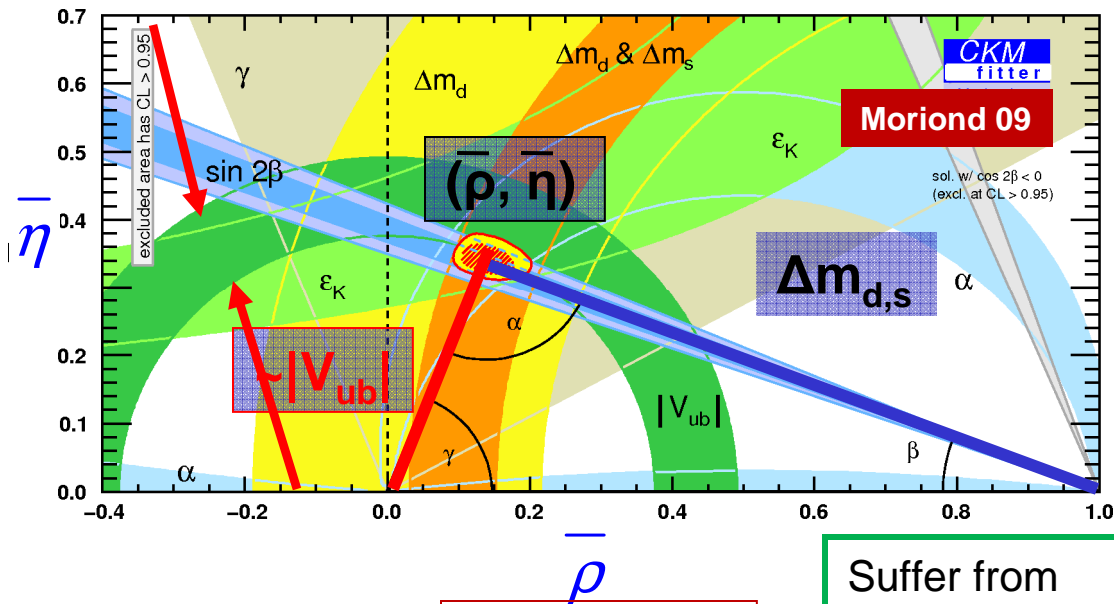
$$\frac{d\Gamma(D \rightarrow K(\pi)e\nu)}{dq^2} = \frac{G_F^2 |V_{cs(cd)}|^2 P_{K(\pi)}^3 |f_+(q^2)|^2}{24\pi^3}, \text{ where } q^2 \equiv M_{e\nu}^2$$

Weak Physics
QCD Physics



- Assuming theoretical calculations of form factors, we can extract  $|V_{cs}|$  and  $|V_{cd}|$
  - Since  $|V_{cs}|$  and  $|V_{cd}|$  are tightly constrained by unitarity, we can check theoretical calculations of the form factors
  - Tested theory can then be applied to B semileptonic decays to extract  $|V_{ub}|$ .
- New modes: to gain a complete understanding of charm semileptonic decays
- $P \rightarrow V$  transitions: 3 hadronic form factors are needed. No unquenched LQCD calculation exists.

# Theory + Experiment = Precision Flavor Physics



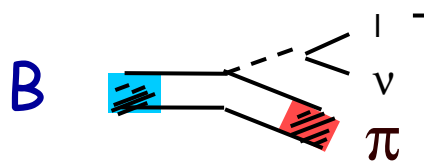
The discovery potential of B physics is limited by systematic errors from QCD (PDG-08):

$$|V_{ub}| = (3.62 \pm 0.22 \pm_{-0.41}^{+0.63}) \times 10^{-3} \pm \text{exp} \pm \text{LQCD}$$

One of the most important goals of B physics

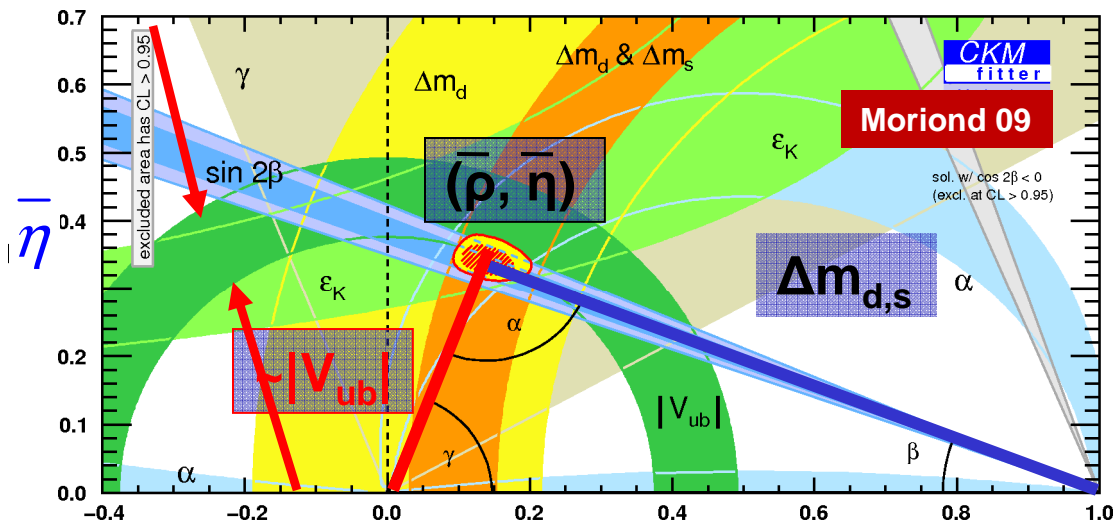
Measured experimentally

Suffer from large theory uncertainty



$$\text{rate} \propto [f^{B \rightarrow \pi}(q^2)]^2 |V_{ub}|^2$$

# Theory + Experiment = Precision Flavor Physics



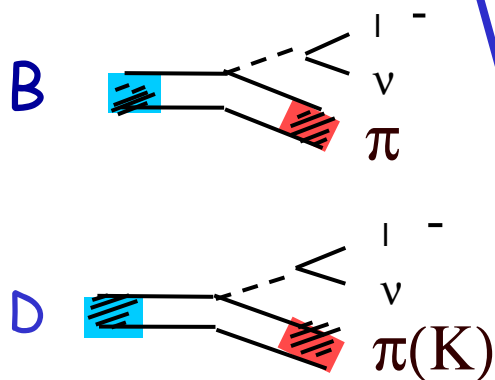
The discovery potential of B physics is limited by systematic errors from QCD (PDG-08):

$$|V_{ub}| = (3.62 \pm 0.22 \pm_{-0.41}^{+0.63}) \times 10^{-3} \pm \text{exp} \pm \text{LQCD}$$

One of the most important goals of B physics

Measured experimentally

Suffer from large theory uncertainty



$$\text{rate} \propto [f^{B \rightarrow \pi}(q^2)]^2 |V_{ub}|^2$$

$$\text{rate} \propto [f^{D \rightarrow \pi(K)}(q^2)]^2 |V_{cd(s)}|^2$$

HQS

Tightly constrained by CKM unitarity

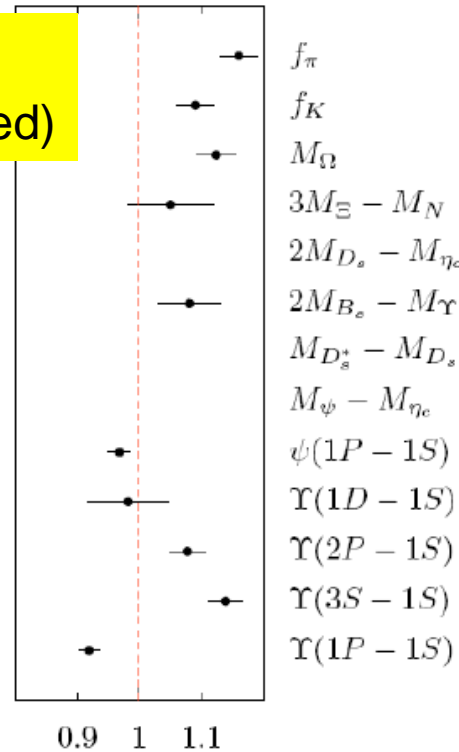
# Theory: A Breakthrough in Lattice QCD

□ Revolutionary progress (2003) in algorithms allows inclusion of QCD vacuum polarization.

□ LQCD demonstrated it can reproduce a wide range of mass differences and decay constants.

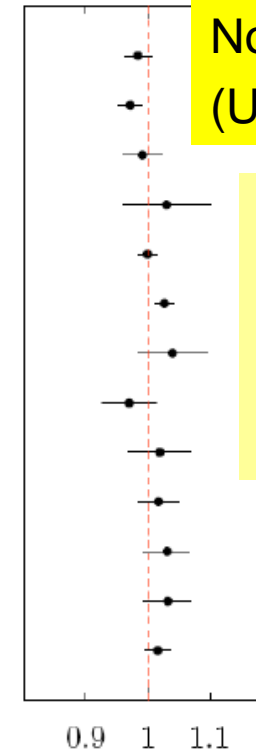
*These were postdictions*

**BEFORE**  
(Quenched)



LQCD/Exp't ( $n_f = 0$ )

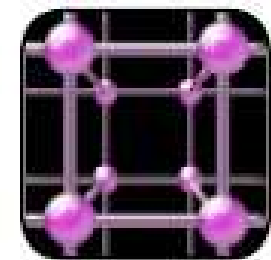
**Now**  
(Unquenched)

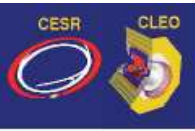


LQCD/Exp't ( $n_f = 3$ )

Phys.Rev.Lett.  
92:022001  
(2004):  
**High-Precision  
Lattice QCD  
Confronts  
Experiment**

- This dramatic improvement needs validation
- *Charm* decay constants  $f_{D^+}$  &  $f_{D_s}$
- *Charm* semileptonic Form factors





# Tagged Analysis Technique at 3770 MeV

- Candidate events are selected by reconstructing a D, called a tag, in several hadronic modes
- Then we reconstruct the semileptonic decay in the system recoiling from the tag
- Two key variables in the reconstruction of a tag:  $\Delta E = E_D - E_{beam}$

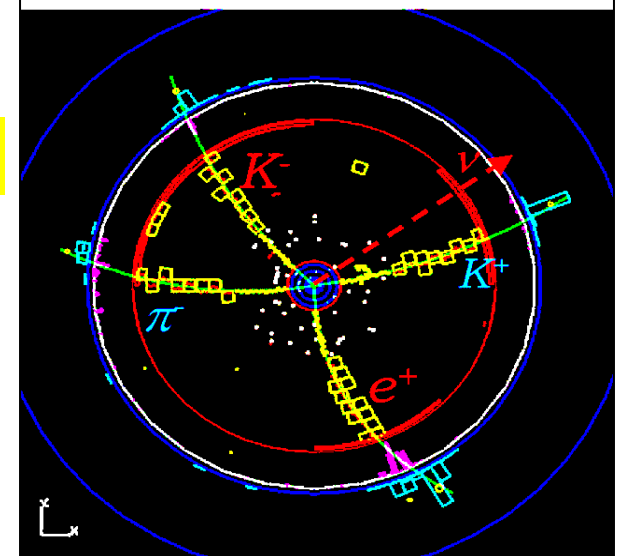
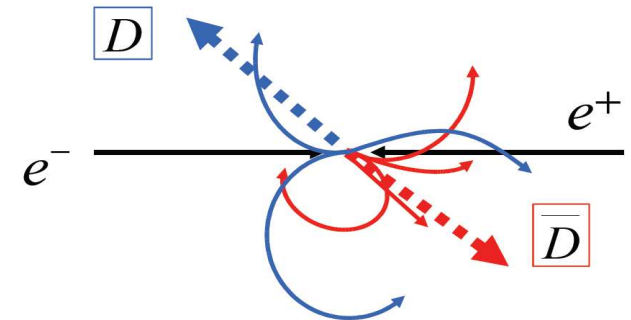
$$M_{bc} = \sqrt{E_{beam}^2/c^4 - |\vec{p}_D|^2/c^2}$$

Tagging creates a single D beam of known 4-momentum

- For semileptonic D:  $U = E_{miss} - |\vec{P}_{miss}|$

U peaks at zero for real semileptonic decays

An **absolute measurement**, independent of the integrated luminosity and number of D mesons in the data sample





# D Tagging at 3770 MeV

World's largest data set at 3.770 GeV

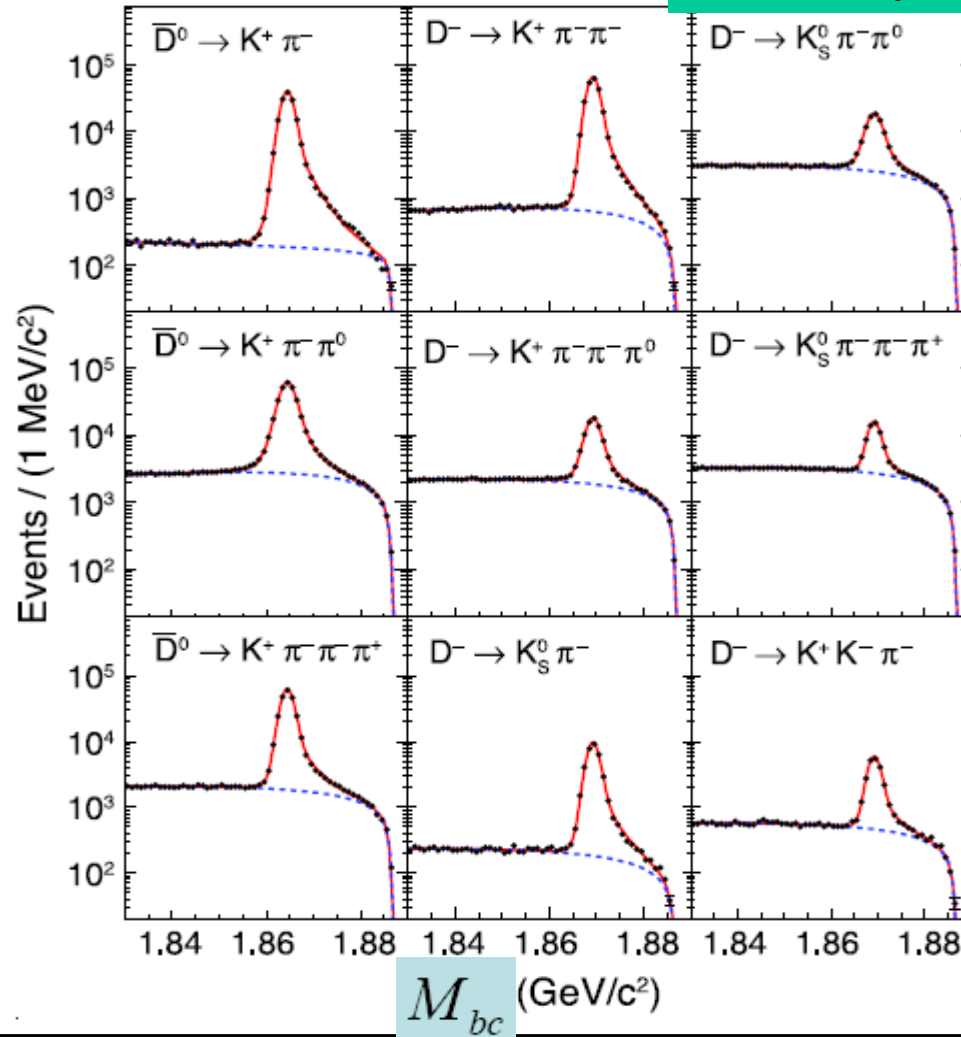
$$M_{bc} = \sqrt{E_{beam}^2/c^4 - |\vec{p}_D|^2/c^2}$$

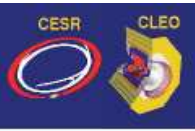
818 pb<sup>-1</sup> @3770 (full data set)  
From the 818 pb<sup>-1</sup>  
D→K/πev analysis

Pure DD,  
zero additional particles,  
~5-6 charged particles per event

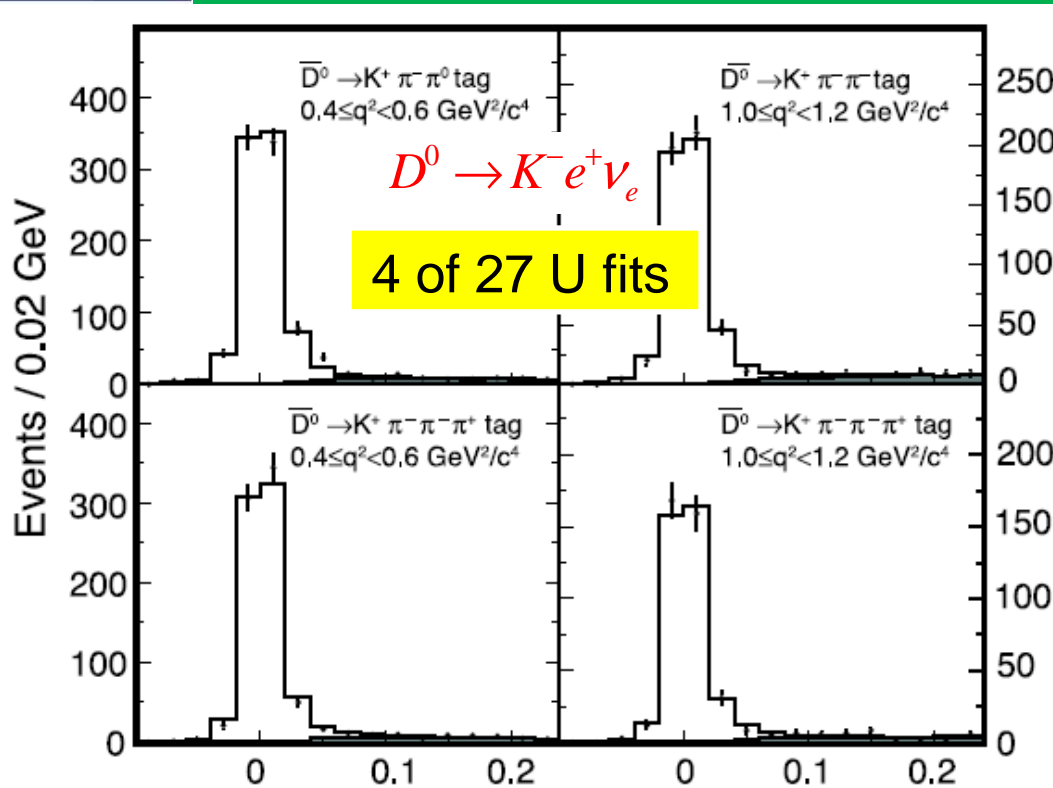
~6.6 × 10<sup>5</sup> D<sup>0</sup> and  
~4.8 × 10<sup>5</sup> D<sup>+</sup> tags  
reconstructed from  
~5.4 × 10<sup>6</sup> DD events

We tag  
~20% of the events,  
compared to  
~0.1% of B's at the  
Y(4S)





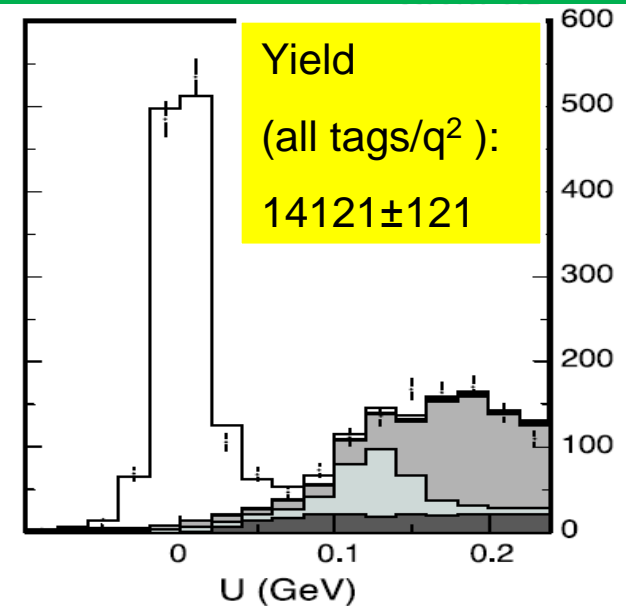
# Fits to the U Distributions for $D \rightarrow K^- e \nu$



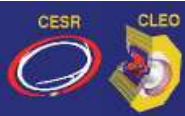
$$U = E_{miss} - c |\vec{P}_{miss}| \text{ (GeV)}$$

Comparisons  
with B  
factories  
follow

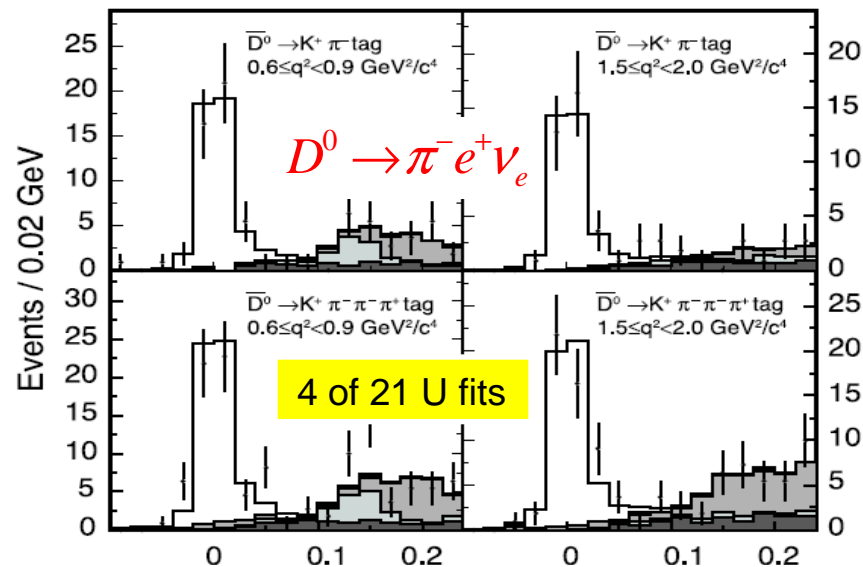
S/N	~300/1
Signal events	~14000
U resolution	~10 MeV
q <sup>2</sup> resolution	~0.008 GeV <sup>2</sup> /c <sup>4</sup>



- We perform binned likelihood fits to U distributions in each  $q^2$  bin and tag mode
- Signal shapes are taken from signal MC, smeared with double Gaussians
- Background shapes are taken from MC with all  $D\bar{D}$  and non- $D\bar{D}$  decays



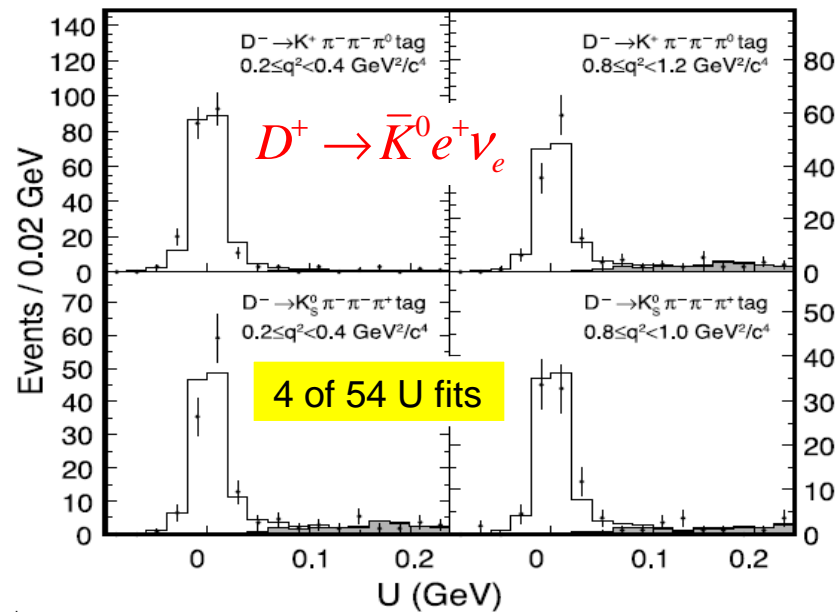
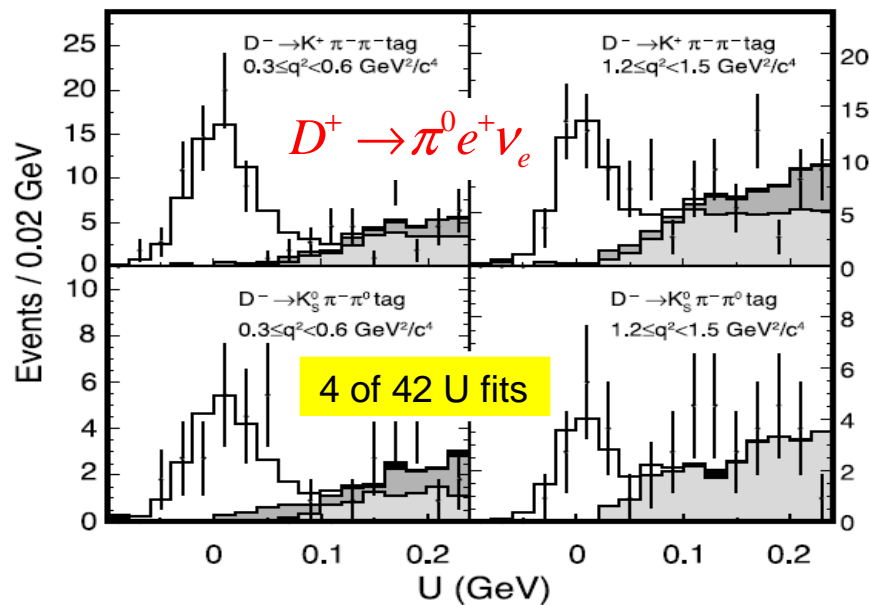
# Fits to the U Distributions for $D \rightarrow \pi^- / \pi^0 / \bar{K}^0 e \bar{\nu}$



$$D^0 \rightarrow \pi^- e^+ \nu_e$$

S/N	~40/1
Signal events	~1400
U resolution	~10 MeV
$q^2$ resolution	~0.008 $\text{GeV}^2/c^4$

Comparisons with B factories on the next two slides



# Form Factor Parameterizations

In general:

$$f_+(q^2) = \frac{f_+(0)}{1-\lambda} \frac{1}{\left(1-q^2/m_{pole}^2\right)} + \frac{1}{\pi} \int_{(m_D+m_P)^2}^{\infty} \frac{\text{Im}(f_+(t))}{t-q^2-i\epsilon} dt$$

Models

- Single pole
- Modified Pole

$$f_+(q^2) = \frac{f_+(0)}{\left(1-q^2/m_{pole}^2\right)}$$

Measure  $f_+(0)$  &  $m_{pole}$

$$f_+(q^2) = \frac{f_+(0)}{\left(1-q^2/m_{pole}^2\right)\left(1-\alpha q^2/m_{pole}^2\right)}$$

Measure  $f_+(0)$  &  $\alpha$

$$m_{pole} = m(D_{(s)}^*)$$

(Allows for additional poles)

independent Model

- Series Expansion

form factors can be written as:

$$f_+(q^2) = \frac{1}{P(q^2)\phi(q^2)} \sum_{k=0}^{\infty} a_k(t_0) [z(q^2, t_0)]^k$$

accounts for  $D_s^*$  pole  $\rightarrow$   $P(q^2)$   $\leftarrow$  ensure  $a_k$ 's good behaviour

$$z(q^2, t_0) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$

$$t_{\pm} \equiv (M_D \pm m_{K,\pi})^2, \quad t_0: \text{arbitrary } q^2 \text{ value that maps to } z=0$$

$z$  is small and converges quickly, linear or quadratic is sufficient to describe the data

Measure  $a_0, r_1 = a_1/a_0, \text{ and } r_2 = a_2/a_0$

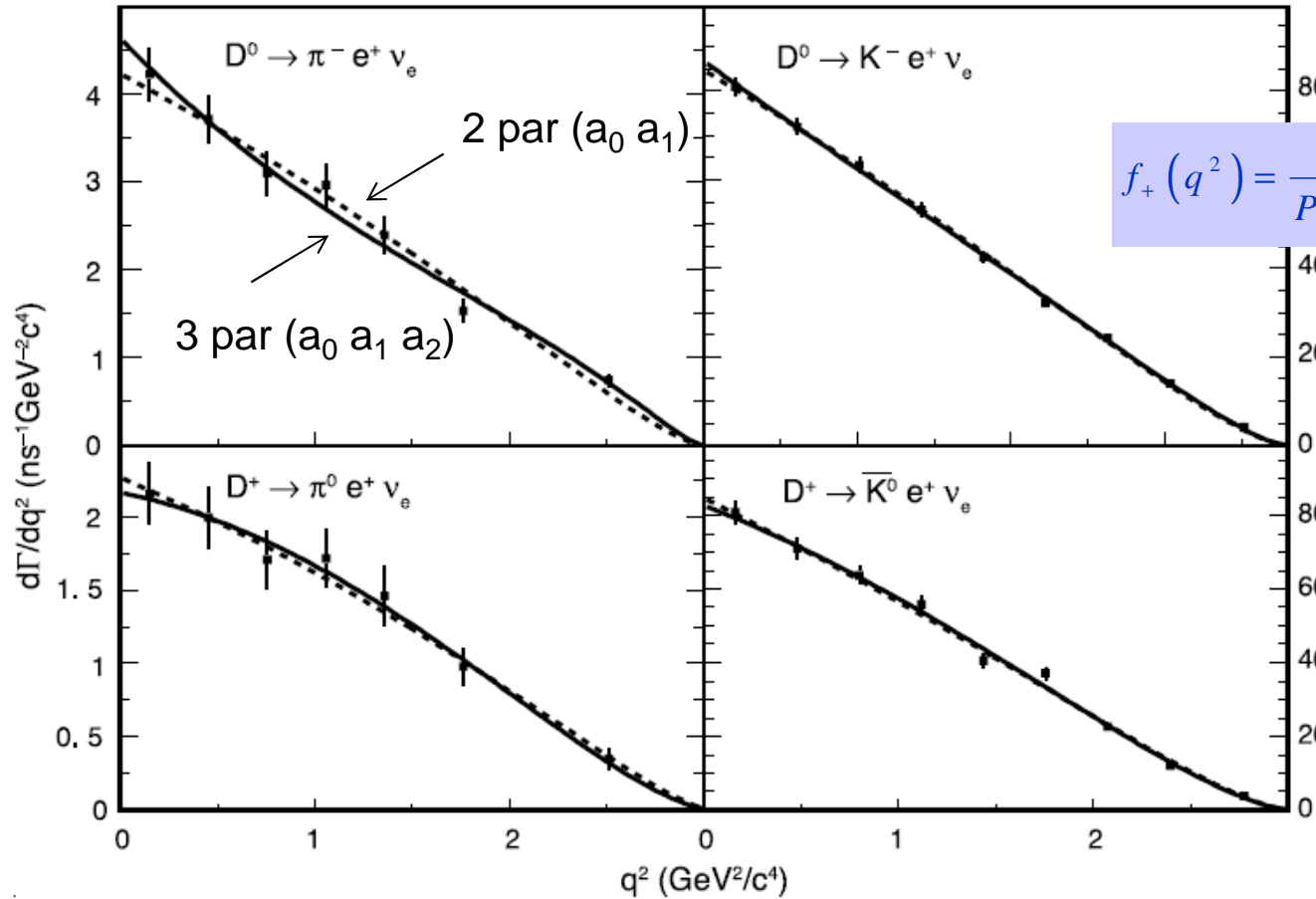
Becher & Hill, *Phys. Lett. B* 633, 61 (2006)



# D → K/π e<sup>+</sup> ν : Fits to the dΓ/dq<sup>2</sup> Distributions

3070109-009

PRD 80, 032005 (2009)



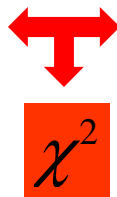
Fit to Becher-Hill Series

$$f_+(q^2) = \frac{1}{P(q^2)\phi(q^2,0)} \left[ \sum_k a_k z^k(q^2,0) \right]$$

Other form factor parameterizations exist, but are only used as functional forms as their physical pictures are not supported by the data

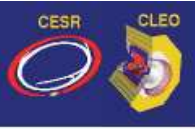
Simultaneous fits to isospin conjugate modes are also performed

Experimentally measured decay rates  $\Gamma_i^{measured}$



Theoretically predicted decay rates

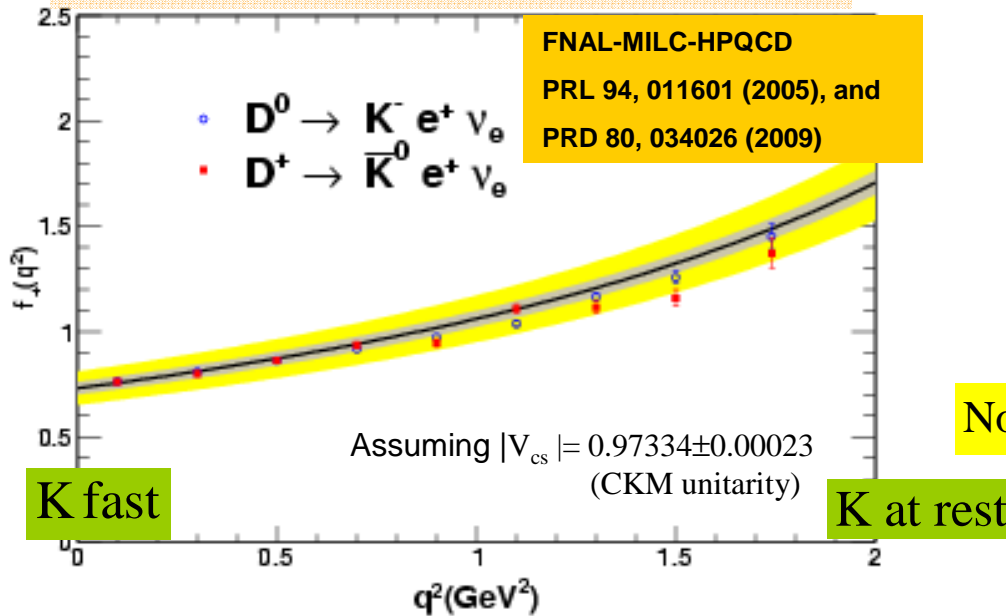
$$\Gamma_i^{predicted} = \int_i d\Gamma = \frac{G_F^2 |V_{Qq'}|^2}{24\pi^3} \int_i |f_+(q^2)|^2 p_P^3 dq^2$$



# D → K e<sup>+</sup>ν Form Factor: Test of LQCD

Form factor measures probability hadron will be formed

$$|V_{cs(cd)}| f_+(q^2) \sim \left[ \frac{\Delta\Gamma_i(D \rightarrow K(\pi)e\nu)}{\Delta q_i^2} / P_{K(\pi)i}^3 \right]^{1/2}$$



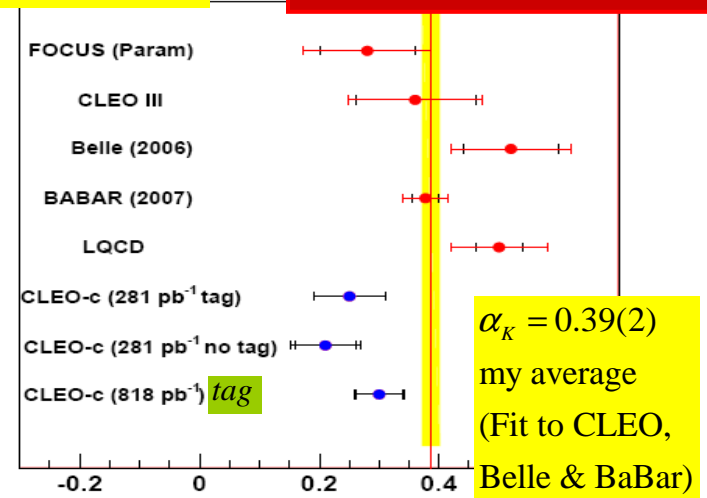
Modified pole model used to compare with LQCD

$$f_+(q^2) = \frac{f_+(0)}{(1 - q^2/m_{pole}^2)(1 - \alpha q^2/m_{pole}^2)}$$

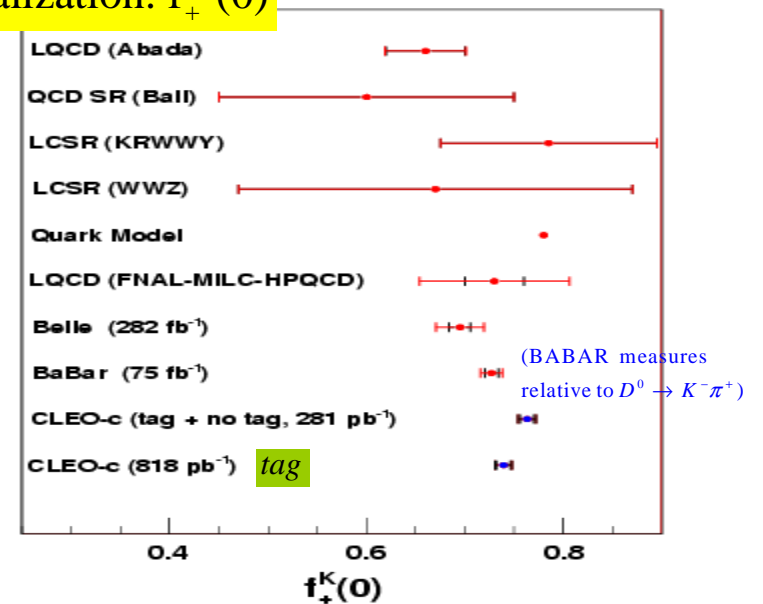
$\alpha$  : CLEO-c prefers smaller value for shape parameter than other experiments  
 $f_+(0)$ : experiments (1.2%) consistent with LQCD (10%)  
 CLEO-c is most precise. *Theoretical precision lags.*

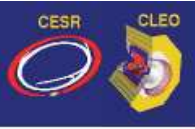
Shape:  $\alpha(K e \nu)$

PRD 80, 032005 (2009)



Normalization:  $f_+^K(0)$

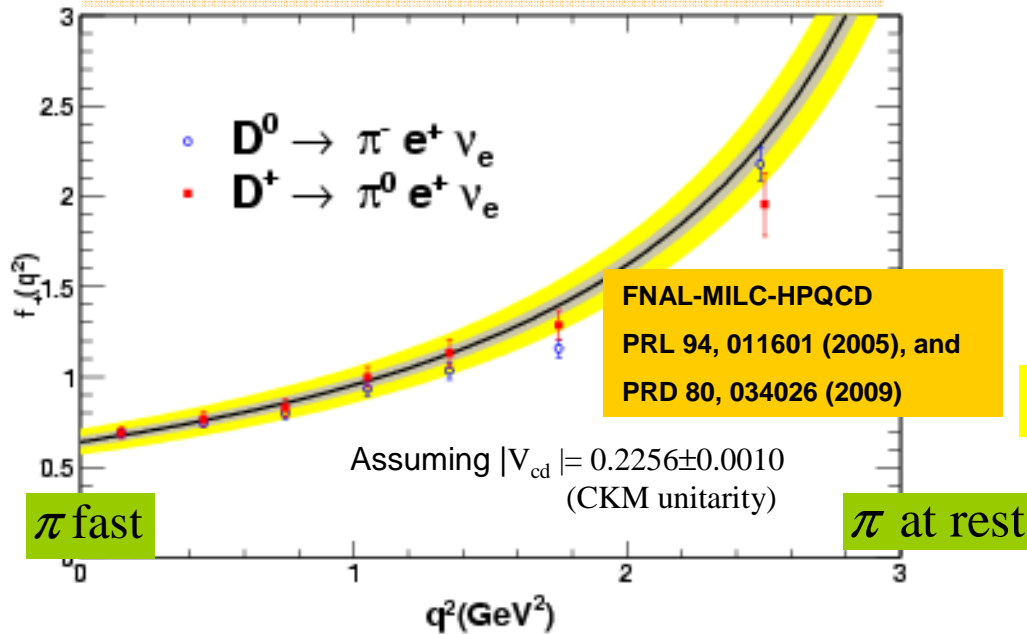




# D → π e<sup>+</sup> ν Form Factor: Test of LQCD

Form factor measures probability hadron will be formed

$$|V_{cs(cd)}| f_+(q^2) \sim \left[ \frac{\Delta\Gamma_i(D \rightarrow K(\pi)e\nu)}{\Delta q_i^2} / P_{K(\pi)i}^3 \right]^{1/2}$$

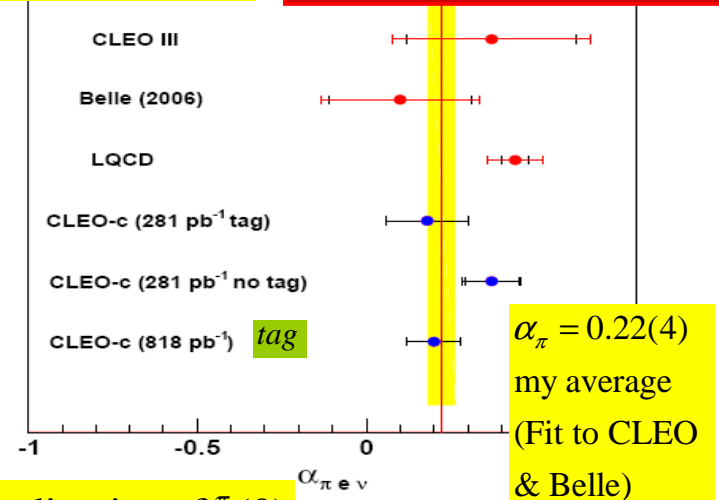


Modified pole model used to compare with LQCD

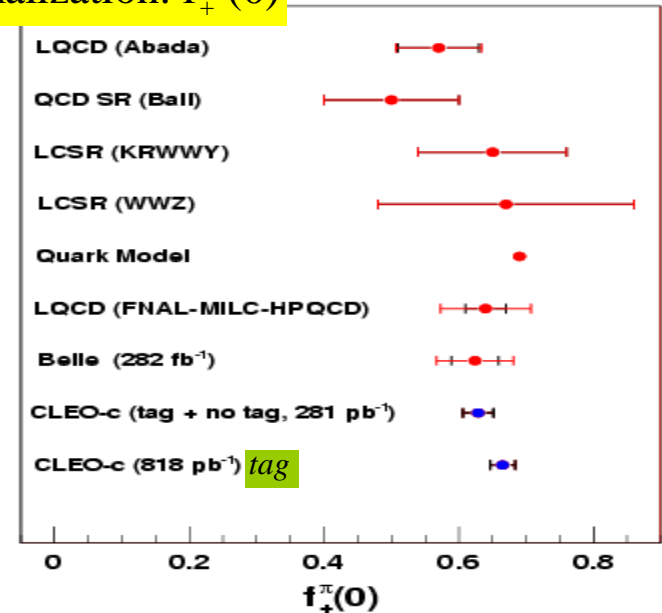
$$f_+(q^2) = \frac{f_+(0)}{(1 - q^2/m_{pole}^2)(1 - \alpha q^2/m_{pole}^2)}$$

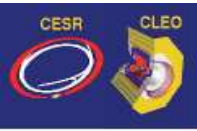
$\alpha$ : CLEO-c measurements are compatible with LQCD  
 $f_+(0)$ : experiments (2.9%) consistent with LQCD (10%).  
 CLEO-c is most precise. *Theoretical precision lags.*

shape:  $\alpha(\pi e\nu)$  — PRD 80, 032005 (2009)



Normalization:  $f_+^\pi(0)$





# $|V_{cs}|$ and $|V_{cd}|$ Results

The data determine  $|V_{cs(d)}|f_+(0)$ .

To extract  $|V_{cs(d)}|$ , we combine the measured  $|V_{cs(d)}|f_+(0)$  values using the Becher-Hill parameterization with (FNAL-MILC-HPQCD) for  $f_+(0)$

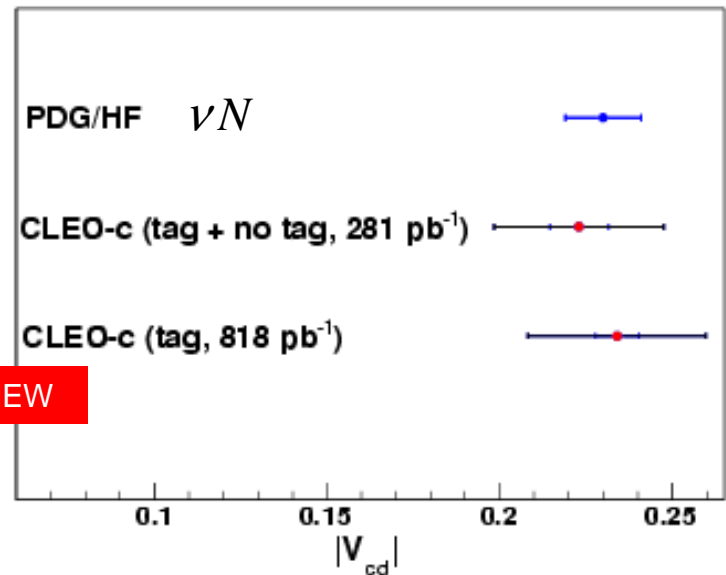
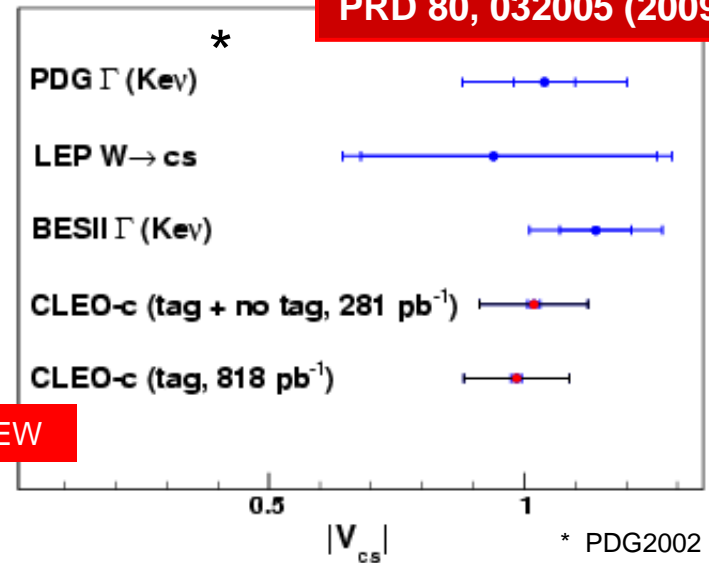
CLEO-c: the most precise *direct* determination of  $|V_{cs}|$   $\sigma(|V_{cs}|)/|V_{cs}| \sim 1.1\%(\text{expt}) \oplus 10\%(\text{theory})$

CLEO - c	$ V_{cs} $
(818 pb <sup>-1</sup> )	$0.985 \pm 0.009 \pm 0.006 \pm 0.103$
	stat    syst    theory

CLEO-c:  $\sigma(|V_{cd}|)/|V_{cd}| \sim 3.1\%(\text{expt}) \oplus 10\%(\text{theory})$   
 $\nu N$  remains most precise determination

CLEO - c	$ V_{cd} $
(818 pb <sup>-1</sup> )	$0.234 \pm 0.007 \pm 0.002 \pm 0.025$
	stat    syst    theory

PRD 80, 032005 (2009)





# Unitarity Test: Compatibility of charm & beauty sectors of CKM matrix?

PRD 80, 052005 (2009)

$|V_{cd}|$  &  $|V_{cs}|$  indirect

1) K & nucleon

$$|V_{ud}| \approx |V_{cs}| \quad \& \quad |V_{cd}| \approx |V_{us}|$$

2) B physics

Indirect = global CKM fit = 1+2

$|V_{cd}|$  &  $|V_{cs}|$  direct

(D semileptonic decays CLEO)

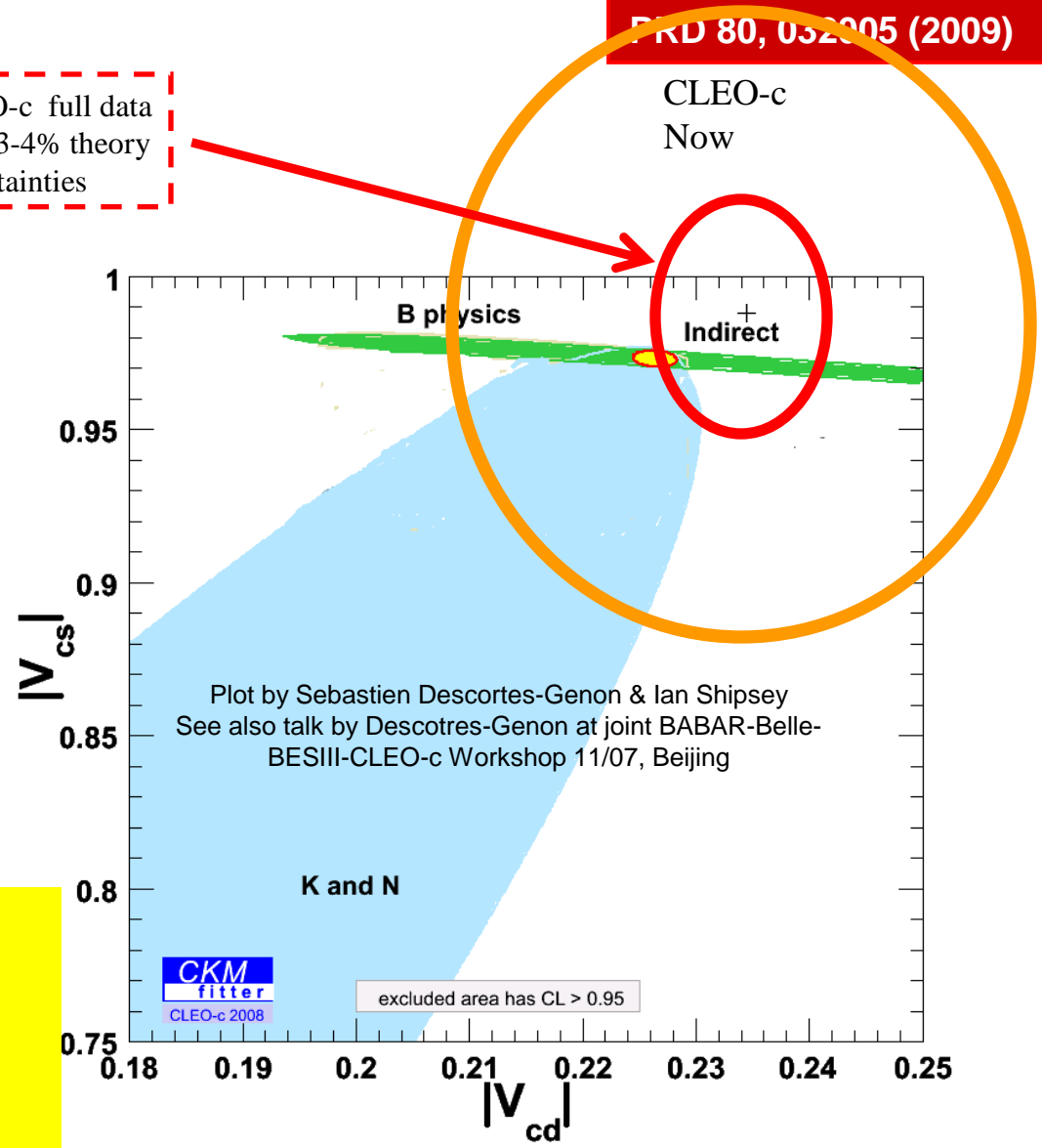
CLEO-c full data set

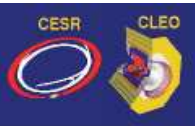
$$\sigma(|V_{cd}|) / |V_{cd}| \sim 3.1\% \oplus \text{theory}$$

$$\sigma(|V_{cs}|) / |V_{cs}| \sim 1.1\% \oplus \text{theory}$$

D semileptonic decays with comparable theory and experimental uncertainty may lead to interesting competition between direct and indirect constraints  
We eagerly await new precise lattice calculations

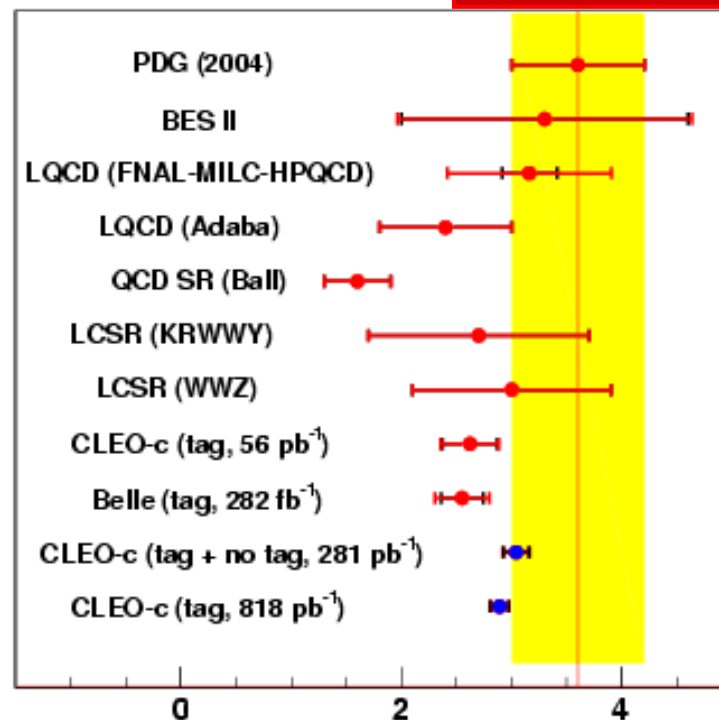
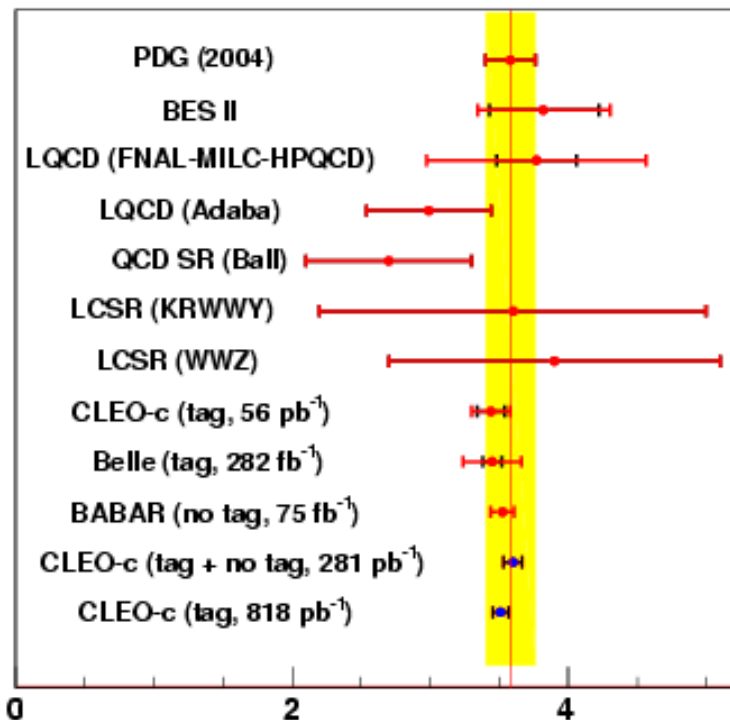
CLEO-c full data set + 3-4% theory uncertainties





# D → K/π e<sup>+</sup>ν Branching fractions

PRD 80, 032005 (2009)



$$B(D^0 \rightarrow K^- e^+ \nu) \times 10^{-2}$$

3.50(3)(4) %

(CLEO-c 818 pb<sup>-1</sup>)

$\sigma(B(Ke\nu)) / B(Ke\nu) \sim 1.4\%$

$\sigma(B(\pi e\nu)) / B(\pi e\nu) \sim 3.0\%$

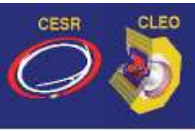
$$B(D^0 \rightarrow \pi^- e^+ \nu) \times 10^{-3}$$

0.288(8)(3) %

(CLEO-c 818 pb<sup>-1</sup>)

Precision measurements from BABAR/Belle/CLEO-c.

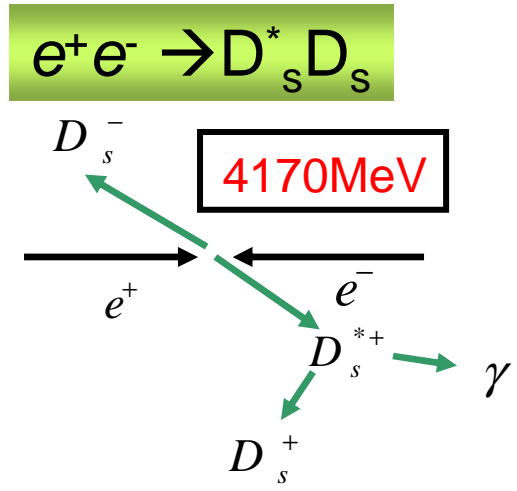
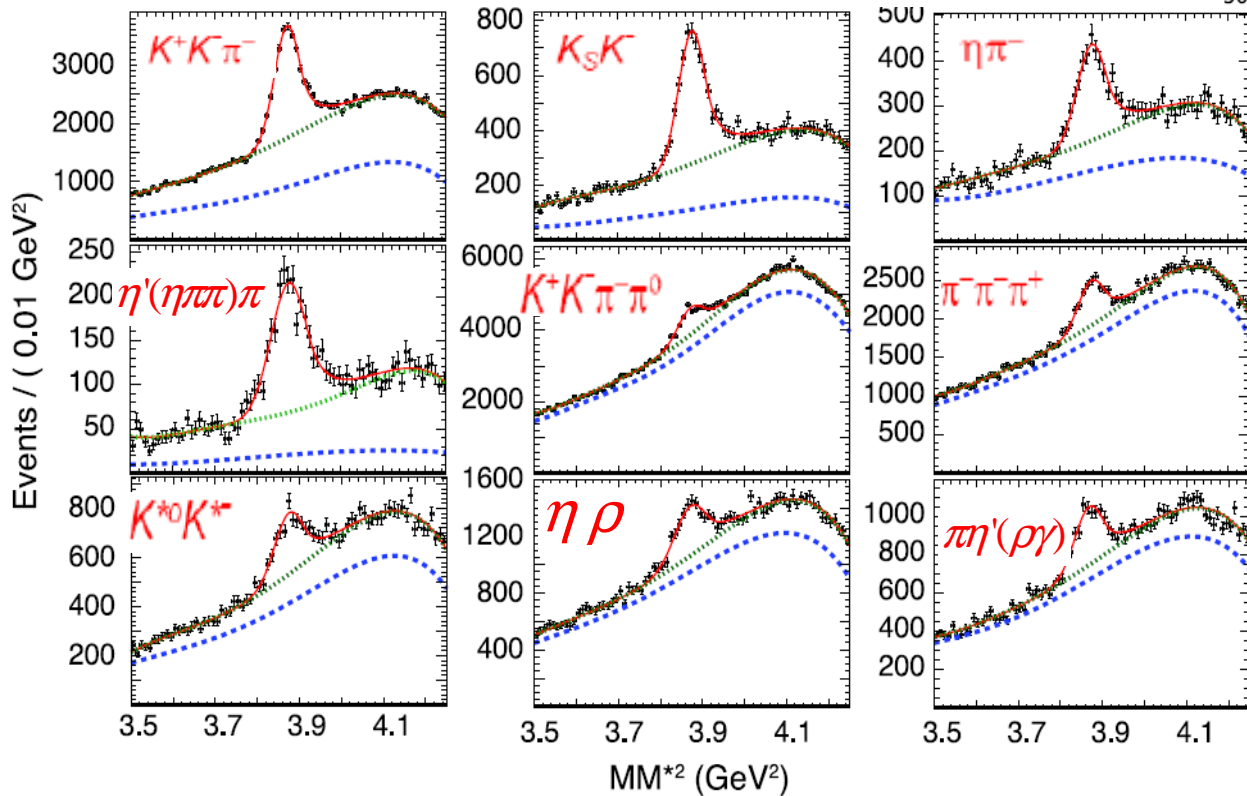
*CLEO-c most precise. Theoretical precision lags experiment.*



# Analysis Technique at 4170 MeV (tagged)

- Candidate events are selected by reconstructing a  $D_s$  in several hadronic modes
- The tag is then combined with a well reconstructed  $\gamma$ , The missing mass squared against the  $\gamma$ -tag pair

$$MM^{*2} = (E_{CM} - E_{D_s(tag)} - E_\gamma)^2 - (\vec{p}_{CM} - \vec{p}_{D_s(tag)} - \vec{p}_\gamma)^2$$



preliminary

9  $D_s$  tag modes:  
 $N(\text{tag}) = 70514 \pm 963$   
 $N(\text{tag} + \gamma) = 43859 \pm 936$   
 reconstructed from  
 $\sim 5.5 \times 10^5 D_s^* D_s$  events

600 pb<sup>-1</sup> @ 4170  
 (CLEO-c full dataset)



# Exclusive $D_s$ Semileptonic Decays

arXiv:0903:0601

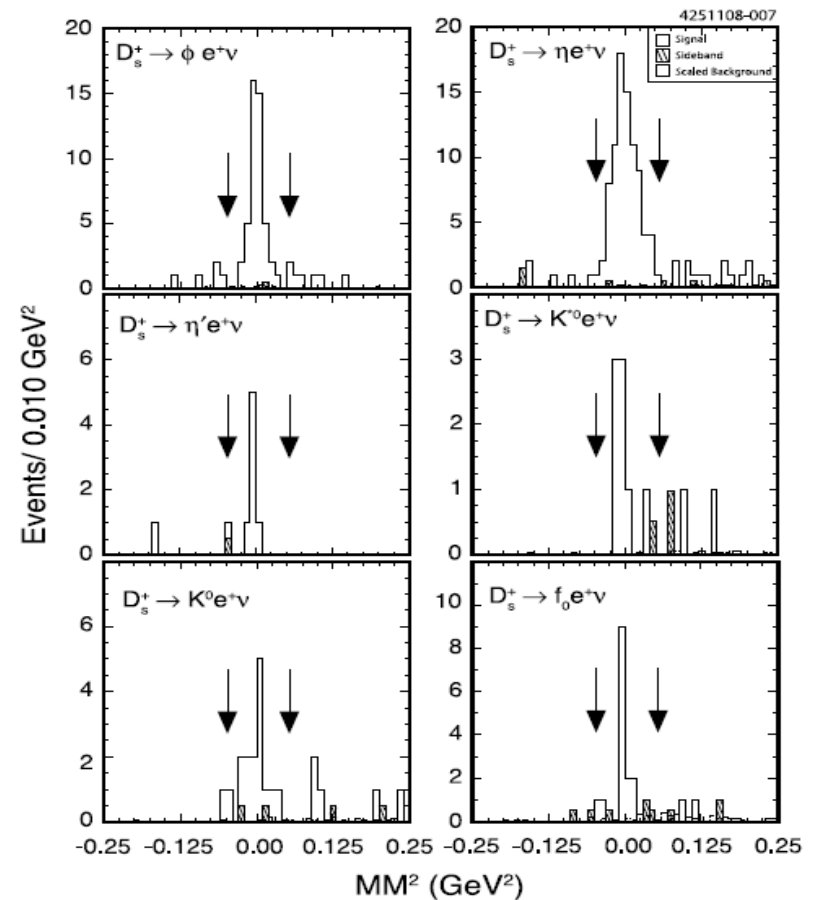
- First absolute branching fraction measurements for  $D_s$  semileptonic decays
- Total width of these exclusive modes is 16% lower than the  $D^0/D^+$  semileptonic widths.
- Shed light on  $\eta$ - $\eta'$ -glueball mixing

**310 pb<sup>-1</sup> @4170  
(Half of full dataset)**

Signal Mode	$\mathcal{B}(\%)$
$D_s^+ \rightarrow \phi e^+ \nu_e$	$2.29 \pm 0.37 \pm 0.11$
$D_s^+ \rightarrow \eta e^+ \nu_e$	$2.48 \pm 0.29 \pm 0.13$
$D_s^+ \rightarrow \eta' e^+ \nu_e$	$0.91 \pm 0.33 \pm 0.05$
$D_s^+ \rightarrow K^0 e^+ \nu_e$	$0.37 \pm 0.10 \pm 0.02$
$D_s^+ \rightarrow K^{*0} e^+ \nu_e$	$0.18 \pm 0.07 \pm 0.01$
$D_s^+ \rightarrow f_0 e^+ \nu_e$	$0.13 \pm 0.04 \pm 0.01$

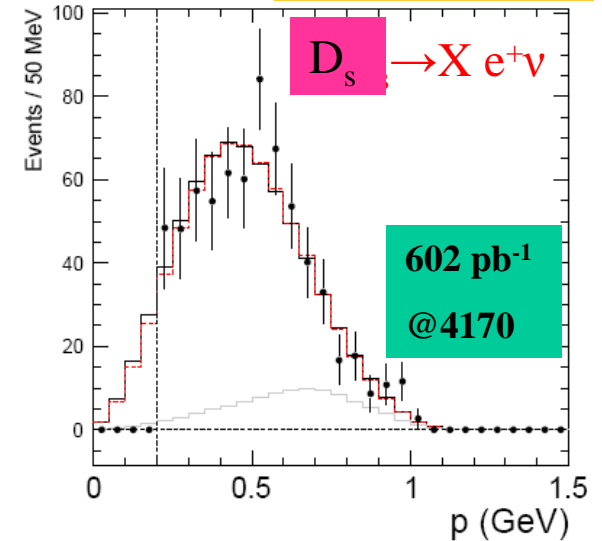
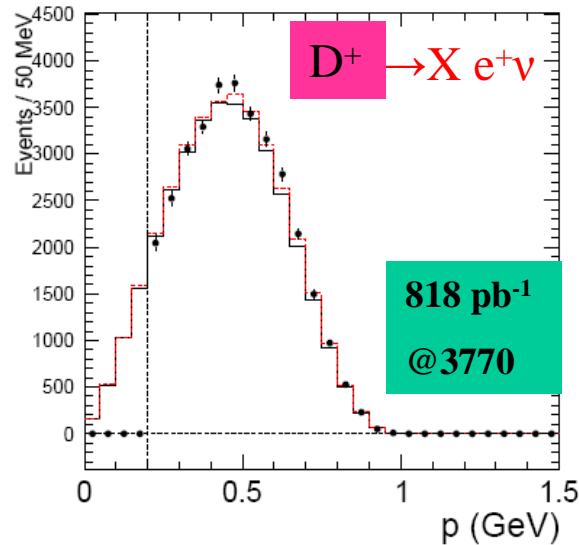
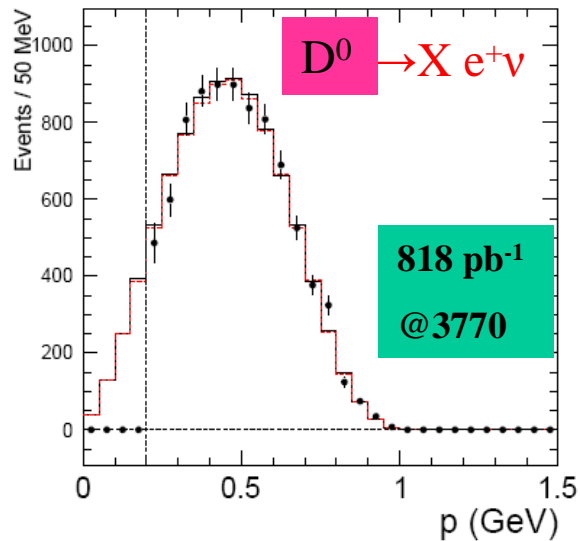
$$MM^2 = (E_{CM} - E_{D_s(tag)} - E_\gamma - E_e - E_{had})^2 - (-\vec{p}_{D_s(tag)} - \vec{p}_\gamma - \vec{p}_e - \vec{p}_{had})^2,$$

in the CM system



# Inclusive Semileptonic Decays of $D^0, D^+,$ and $D_s$

PRELIMINARY



	$D^0 \rightarrow X e^+ \nu$	$D^+ \rightarrow X e^+ \nu$	$D_s \rightarrow X e^+ \nu$
Inclusive B (%)	$6.55 \pm 0.10 \pm 0.09$	$16.36 \pm 0.11 \pm 0.29$	$6.49 \pm 0.40 \pm 0.18$
Sum of exclusive B (%)	$6.1 \pm 0.2 \pm 0.2$	$15.1 \pm 0.5 \pm 0.5$	$6.47 \pm 0.60$

□ Use knowledge of D semileptonic decay to extrapolate below the momentum cutoff (200 MeV/c)

Any additional exclusive modes will have small branching ratios

$$\Gamma_{D^+}^{SL} / \Gamma_{D^0}^{SL} = 0.99 \pm 0.02 \pm 0.02 \quad \text{Isospin symmetry}$$

$$\Gamma_{D_s^+}^{SL} / \Gamma_{D^0}^{SL} = 0.81 \pm 0.05 \pm 0.03 \quad \text{SU(3) is broken}$$

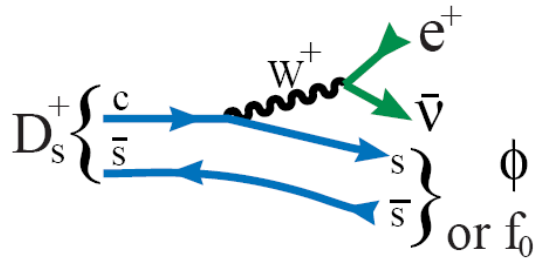


# $D_s^+ \rightarrow f_0(980)e^+\nu$

arXiv: 0907.3201  
(submitted to PRD)

600 pb<sup>-1</sup> @4170  
(CLEO-c full dataset)

- $D_s$  semileptonic decays provide a very clean environment to study the properties of the  $f_0(980)$  meson
- Implications for quark content of  $f_0$
- It is suggested that  $B_s \rightarrow J/\psi f_0$  can be an alternative to  $B_s \rightarrow J/\psi \phi$  to measure CP Violation in the  $B_s$  system Stone & Zhang [PRD79, 074024]



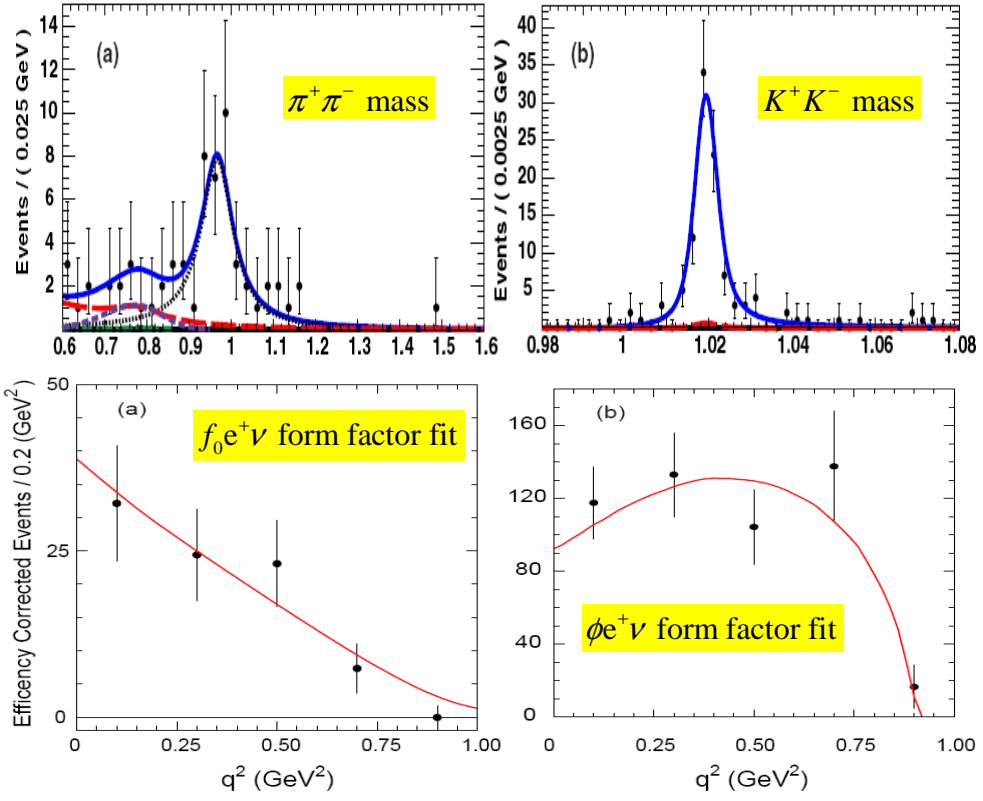
□ Many interesting results:

- ✓  $\text{Br}(D_s^+ \rightarrow f_0(980)e^+\nu, f_0 \rightarrow \pi^+\pi^-) = (0.20 \pm 0.03 \pm 0.01)\%$
- ✓  $\text{Br}(D_s^+ \rightarrow \phi e^+\nu) = (2.36 \pm 0.23 \pm 0.13)\%$

$$\frac{\left. \frac{d\text{Br}}{dq^2}(D_s^+ \rightarrow f_0(980)e^+\nu) \text{Br}(f_0 \rightarrow \pi^+\pi^-) \right|_{q^2=0}}{\left. \frac{d\text{Br}}{dq^2}(D_s^+ \rightarrow \phi e^+\nu) \text{Br}(\phi \rightarrow K^+K^-) \right|_{q^2=0}} = (42 \pm 11)\%$$

$$\left[ \text{Predicted to equal } \frac{\text{Br}(B_s \rightarrow J/\psi f_0) \text{Br}(f_0 \rightarrow \pi^+\pi^-)}{\text{Br}(B_s \rightarrow J/\psi \phi) \text{Br}(\phi \rightarrow K^+K^-)} \right]$$

- ✓  $M_{f_0(980)} = (977_{-9}^{+11} \pm 1)\text{MeV}, \Gamma_{f_0(980)} = (91_{-22}^{+30} \pm 3)\text{MeV}$
- ✓ Simple pole model  $M_{\text{pole}} = (1.7_{-0.7}^{+4.5} \pm 0.2)\text{GeV}$



# Summary

- ❑ Charm semileptonic decays are an excellent test ground of LQCD.
  - ❑  $D \rightarrow Ke^+\nu$ ,  $D \rightarrow \pi e^+\nu$  form factors in general agreement with LQCD.
- ❑ Measured to better precision than LQCD.
  - ❑ CLEO-c measures form factor normalizations for  $D \rightarrow Ke^+\nu$ ,  $D \rightarrow \pi e^+\nu$  to 3% and 1%, respectively, while LQCD predicts them at 10% level.
- ❑ Direct measurements of CKM elements.
  - ❑ Best direct measurement of  $|V_{cs}|$ , measured to  $\pm 1.1\%$ (experimental)  $\pm 10\%$ (theory).
  - ❑  $|V_{cd}|$  is measured to  $\pm 3.1\%$ (experimental)  $\pm 10\%$ (theory).
- ❑ Recent measurements of  $D_s$  semileptonic measurements with tagged data sets.
  - ❑ Measurement of 6 exclusive semileptonic branching fractions.
  - ❑ First direct evidence of a semileptonic decay with scalar meson in the final state.
  - ❑ Form factor measurement for  $D_s \rightarrow f_0(980)e^+\nu$
  
- ❑ Thanks again to Bo Xin and Ian Shipsey